#### Algebra I **Conceptual Category: A: Algebra** Pacing Date(s) Traditional 21 days 01/29/14-02/28/14 **Topic IX:** Polynomials 01/29/14-02/28/14 Block 10 davs **COMMON CORE STATE NEXT GENERATION SUNSHINE** STANDARD(S) & ESSENTIAL CONTENT OBJECTIVES STATE STANDARD(S) **MATHEMATICAL PRACTICE (MP)** MACC. 912. A-APR.1.1: Understand that MA.912.A.4.1: Simplify monomials and NGSSS POLYNOMIALS monomial expressions using the laws of polynomials form a system analogous to the integers, namely, they are closed integral exponents. (EOC) Polynomials terminology • A. Simplify Monomial Expressions under the operations of addition, ٠ Identify a monomial, binomial, trinomial, and a 1. Properties of Exponents subtraction, and multiplication; add, MA.912.A.4.2: Add, subtract, and multiply polynomial Multiplication i. subtract, and multiply polynomials. (MP.2, polynomials (FI, EOC) • Apply properties of exponents to simplify ii. Division MP.7) polynomial expressions MA.912.A.4.3: Factor polynomial Expand a binomial expression and combine B. Multiplying Polynomials • MACC.912.A-SSE.1.2: Use the structure expressions (EOC) like terms 1. Special Products of of an expression to identify ways to rewrite Polynomials Factor polynomial expressions, which may ٠ it. For example, see x4 - y4 as (x2)2 - y4MA.912.A.4.4: Divide polynomials by include a GCF. difference of two squares, and $(\sqrt{2})^2$ , thus recognizing it as a difference of monomials. (EOC) C. Dividing Polynomials trinomials squares that can be factored as (x2 -Dividing Polynomials by Simplify algebraic ratios 1. • y2)(x2 + y2). (MP.1, MP.2, MP.4, MP.7) Monomials Divide polynomials by monomials MACC. 912.A-SSE.2.3: Choose and **D.** Factoring Polynomials produce an equivalent form of an Factoring by GCF 1. expression to reveal and explain properties 2. Factoring Trinomials of the quantity represented by the 3. Factoring Special expression.(MP.2, MP.7) Products FI: Fall Interim

EOC: End Of Course

WI: Winter Interim

Course Code: 120031001

#### Algebra I

#### Course Code: 120031001

#### **INSTRUCTIONAL TOOLS**

#### Core Text Book: Prentice Hall Algebra 1. Honors Gold Series Florida

Benchmark	Suggested Lessons	Teacher Notes
MA.912.A.4.1	7.1, 7.3, 7.4, 7.5	
MA.912.A.4.2	8.1, 8.2, 8.3, 8.4	
MA.912.A.4.3	8.2, 8.5, 8.6, 8.7, 8.8	
MA.912.A.4.4	11.3	

#### Notes:

The order in which the standards and suggested lessons are listed is not necessary the order of instruction. Please review each section during your instructional planning and supplement or modify components as needed to best differentiate instruction.

Use Algebra 1 EOC Item Specifications as a resource document to help define grade-level content.

Vocabulary: monomial, polynomial, factor, greatest common factor (GCF), greatest monomial factor (GMF), difference of squares, perfect square trinomial, distributive property

#### Instructional Strategies:

The primary strategy for this cluster is to make connections between arithmetic of integers and arithmetic of polynomials. In order to understand this standard, students need to work toward both understanding and fluency with polynomial arithmetic. Furthermore, to talk about their work, students will need to use correct vocabulary, such as integer, monomial, polynomial, factor, and term.

In arithmetic of polynomials, a central idea is the distributive property, because it is fundamental not only in polynomial multiplication but also in polynomial addition and subtraction.

With the distributive property, there is little need to emphasize *misleading mnemonics*, such as FOIL, which is relevant only when multiplying two binomials, and the procedural reminder to "collect like terms" as a consequence of the distributive property. For example, when adding the polynomials 3x and 2x, the result can be explained with the distributive property as follows: 3x + 2x = (3 + 2)x = 5x.

For polynomials, students need to reason that the sum (difference or product) of any two polynomials is indeed a polynomial. At first, restrict attention to polynomials with integer coefficients. Later, students should consider polynomials with rational or real coefficients and reason that such polynomials are closed under these operations.

For contrast, students need to reason that polynomials are not closed under the operation of division: The quotient of two polynomials is not always a polynomial. For example

 $(x^2 + x) \div x$  is not a polynomial. Of course, the quotient of two polynomials is sometimes a polynomial. For example,  $(x^2 - 9) \div (x - 3) = x + 3$ .

Hands-on materials, such as algebra tiles, can be used to establish a visual understanding of algebraic expressions and the meaning of terms, factors and coefficients. Technology may be useful to help a student recognize that two different expressions represent the same relationship. For example, since (x - y)(x + y) can be rewritten as  $x^2 - y^2$ , they can put both expressions into a graphing calculator (or spreadsheet) and have it generate two tables (or two columns of one table), displaying the same output values for each expression.

### Algebra I

# Course Code: 120031001

COMMON CORE STATE STANDARDS				
MATHEMATICAL PRACTICES				
DESCRIPTION				
MACC.K12.MP.1 (back to top) Make sense of problems and persevere in solving them.	<ul> <li>Mathematically proficient students will be able to:</li> <li>Explain the meaning of a problem and looking for entry points to its solution.</li> <li>Analyze givens, constraints, relationships, and goals.</li> <li>Make conjectures about the form and meaning of the solution and plan a solution pathway.</li> <li>Consider analogous problems, and try special cases and simpler forms of the original problem in order to gain insight into its solution.</li> <li>Monitor and evaluate their progress and change course if necessary.</li> <li>Explain correspondences between equations, verbal descriptions, tables, and graphs or draw diagrams of important features and relationships, graph data, and search for regularity or trends.</li> <li>Check answers to problems using a different method, and continually ask, "Does this make sense?"</li> <li>Identify correspondences between different approaches.</li> </ul>			
MACC.K12.MP.2 (back to top) Reason abstractly and quantitatively.	<ul> <li>Mathematically proficient students will be able to:</li> <li>Make sense of quantities and their relationships in problem situations.</li> <li>Decontextualize—to abstract a given situation and represent it symbolically.</li> <li>Contextualize, to pause as needed during the manipulation process in order to probe into the referents for the symbols</li> <li>Create a coherent representation of the problem at hand; considering the units involved; attending to the meaning of quantities, not just how to compute them.</li> <li>Know and be flexible using different properties of operations and objects.</li> </ul>			
MACC.K12.MP.3 (back to top) Construct viable arguments and critique the reasoning of others.	<ul> <li>Mathematically proficient students will be able to:</li> <li>Understand and use stated assumptions, definitions, and previously established results in constructing arguments.</li> <li>Make conjectures and build a logical progression of statements to explore the truth of their conjectures.</li> <li>Analyze situations by breaking them into cases, and can recognize and use counterexamples.</li> <li>Justify their conclusions, communicate them to others, and respond to the arguments of others.</li> <li>Reason inductively about data, making plausible arguments that take into account the context from which the data arose.</li> <li>Compare the effectiveness of two plausible arguments, distinguish correct logic or reasoning from that which is flawed, and—if there is a flaw in an argument—explain what it is.</li> <li>Determine domains to which an argument applies.</li> </ul>			
MACC.K12.MP.4 (back to top) Model with mathematics.	<ul> <li>Mathematically proficient students will be able to:</li> <li>Apply the mathematics they know to solve problems arising in everyday life, society, and the workplace.</li> <li>Use geometry to solve a design problem or use a function to describe how one quantity of interest depends on another.</li> <li>Apply what they know and feel comfortable making assumptions and approximations to simplify a complicated situation, realizing that these may need revision later.</li> <li>Identify important quantities in a practical situation and map their relationships using such tools as diagrams, two-way tables, graphs, flowcharts and formulas.</li> <li>Analyze relationships mathematically to draw conclusions.</li> <li>Interpret mathematical results in the context of the situation and reflect on whether the results make sense, possibly improving the model if it has not served its purpose.</li> </ul>			

### Algebra I

Course Code: 120031001

	COMMON CORE STATE STANDARDS			
MATHEMATICAL PRACTICES				
DESCRIPTION				
MACC.K12.MP.5 (back to top) Use appropriate tools strategically.	<ul> <li>Mathematically proficient students will be able to:</li> <li>Consider the available tools when solving a mathematical problem. These tools might include pencil and paper, concrete models, a ruler, a protractor, a calculator, a spreadsheet, a computer algebra system, a statistical package, or dynamic geometry software.</li> <li>Make sound decisions about when each of the tools appropriate for their grade or course might be helpful, recognizing both the insight to be gained and their limitations. Example: High school students analyze graphs of functions and solutions using a graphing calculator.</li> <li>Detect possible errors by strategically using estimation and other mathematical knowledge.</li> <li>Know that technology can enable them to visualize the results of varying assumptions, explore consequences, and compare predictions with data.</li> <li>Identify relevant external mathematical resources, such as digital content located on a website, and use them to pose or solve problems.</li> <li>Use technological tools to explore and deepen their understanding of concepts</li> </ul>			
MACC.K12.MP.6 (back to top) Attend to precision.	<ul> <li>Mathematically proficient students will be able to:</li> <li>Communicate precisely to others.</li> <li>Use clear definitions in discussion with others and in their own reasoning.</li> <li>State the meaning of the symbols they choose, including using the equal sign consistently and appropriately.</li> <li>Be careful about specifying units of measure, and labeling axes to clarify the correspondence with quantities in a problem.</li> <li>Calculate accurately and efficiently, express numerical answers with a degree of precision appropriate for the problem context.</li> </ul>			
MACC.K12.MP.7 (back to top) Look for and make use of structure.	<ul> <li>Mathematically proficient students will be able to:</li> <li>Discern a pattern or structure. Example: In the expression x<sup>2</sup> + 9x + 14, students can see the 14 as 2 x 7 and the 9 as 2 + 7.</li> <li>Recognize the significance of an existing line in a geometric figure and can use the strategy of drawing an auxiliary line for solving problems. Step back for an overview and shift perspective.</li> <li>See complicated things, such as some algebraic expressions, as single objects or as being composed of several objects. Example: They can see 5 - 3(x - y)<sup>2</sup> as 5 minus a positive number times a square and use that to realize that its value cannot be more than 5 for any real numbers x and y.</li> </ul>			
MACC.K12.MP.8 (back to top) Look for and express regularity in repeated reasoning.	<ul> <li>Mathematically proficient students will be able to:</li> <li>Notice if calculations are repeated, and look both for general methods and for shortcuts. Example: Noticing the regularity in the way terms cancel when expanding (x-1)(x+1),(x-1)(x2+x+1),and(x-1)(x3 +x2+x+1)might lead them to the general formula for the sum of a geometric series.</li> <li>Maintain oversight of the process, while attending to the details as they work to solve a problem.</li> <li>Continually evaluate the reasonableness of their intermediate results.</li> </ul>			

#### Algebra I

# Course Code: 120031001

## **NEXT GENERATION SUNSHINE STATE STANDARDS**

**Standard 4: Linear Polynomials:** Students solve linear equations and inequalities. Perform operations on polynomials. Find factors of polynomials, learning special techniques for factoring quadratics.

BENCHMARK CODE	BENCHMARK DESCRIPTION				
MA.912.A.4.1 (back to top)	Simplify monomials and monomial expressions using the laws of integral exponents.				
MC/FR	Remarks/ExamplesExample 1: SimplifyExample 3: Simplify:Example 6: Simplify: $(3a^3)(12a^2)$ $(3z^4)^3$ $10$				
	$ \begin{array}{c} (3a^3)(12a^2) \\ \text{Example 2: Simplify:} \end{array}  \begin{array}{c} (3z^4)^3 \\ \text{Example 4: Simplify:} \end{array}  \begin{array}{c} 10 \\ x^{-4} \end{array} $				
	$\frac{15x^7}{3x^5}, x \neq 0$ $\frac{(a^0)}{(3xy)^3}, a \neq 0$ Example 7: Simplify: $\left(\frac{a^2b^5}{ab^2}\right), a \neq 0, b \neq 0$				
	<u>Cognitive Complexity</u> : Low				
	Clarification (EOC): Students will apply the laws of exponents to simplify monomials and monomial expressions with integral exponents.				
	<ul> <li>Content Limits (EOC):</li> <li>Exponents should adhere to the general content limits.</li> <li>Items must have a variable base and may include a numerical base.</li> <li>Monomials may have no more than three variables.</li> <li>Items may use negative exponents.</li> </ul>				
MA.912.A.4.2	Add, subtract, and multiply polynomials				
(back to top)	$\frac{Remarks/Examples}{Example 1: (4x^2 - 7x + 2) - (x^2 + 4x - 5) = ?}$				
MC/FR	Example 2: $(n + 2)(4n - 5) = ?$				
	<u>Cognitive Complexity</u> : Low				
	Clarification (EOC): Students will simplify (add, subtract, and multiply) polynomial expressions.				
	<ul> <li>Content Limits (EOC):</li> <li>Items requiring multiplication of polynomials are limited to a product of: two monomials, a monomial and a binomial, a monomial and a trinomial, or two binomials.</li> </ul>				
	• Items requiring addition and subtraction are limited to combining monomials, binomials, and/or trinomials. The simplified sum or difference should contain no more than five terms.				

### Algebra I

Course Code: 120031001

Standard 4: Linear Polynomials: Students solve linear equations and inequalities. Perform operations on polynomials. Find factors of polynomials, learning special techniques for factoring quadratics.

BENCHMARK CODE	BENCHMARK DESCRIPTION			
MA.912.A.4.3 (back to top)	Factor polynomial expressions.			
	<u>Remarks/Examples:</u>			
МС	Example 1: Factor Example 2: Factor			
WC	$36xy^2 + 18xy^4 - 12x^2y^4 \qquad \qquad 2x^2 - 7x + 3$			
	<ul> <li><u>Cognitive Complexity</u>: Moderate</li> <li><u>Clarification (EOC)</u>: Students will completely factor polynomial expressions, which may include a greatest common factor, difference of two squares, and trinomials. Students will use factoring methods to simplify rational expressions. (Also assesses MA.912.A.5.1)</li> <li><u>Content Limits (EOC)</u>:         <ul> <li>All monomials in items will have, at most, two variables.</li> <li>Coefficients must be integers.</li> <li>In items requiring first factoring the greatest common factor and then factoring the remaining polynomial, the remaining polynomial must have a maximum degree of two.</li> </ul> </li> </ul>			
MA.912.A.4.4 (back to top) MC	Divide polynomials by monomials. $\frac{Remarks/Examples:}{Example 1:}$ Simplify $\frac{4x^3y^2 + 8xy^4 - 6x^2y^5}{2xy^2}$ Cognitive Complexity: Moderate Clarification (EOC): Students will divide polynomials by monomials.			
	<ul> <li>Content Limits (EOC):</li> <li>Items will be limited to dividing a polynomial by a monomial.</li> <li>Synthetic division will not be assessed.</li> </ul>			

Algebra I

Course Code: 120031001

**TECHNOLOGY TOOLS** 

 FLORIDA FOCUS
 http://focus.florida-achieves.com

 Sign-in and Password: First 4 letters of Last Name and Last 4 Digits Employee Number. Example: abcd1234

 MA.912.A.4.1

 MA.912.A.4.2

 MA.912.A.4.3

 MA.912.A.4.4

GRAPHING CALCULATOR ACTIVITIES			
CONTENT FOCUS TITLE SITE			
Polynomiala	Factored Polynomials	http://education.ti.com/educationportal/activityexchange/Activity.do?cid=US&ald=6168	
Polynomials	Multiplying Binomials	http://education.ti.com/educationportal/activityexchange/Activity.do?cid=US&aId=6036	

GIZMO CORRELATION	
GIZMO TITLE	
Modeling the Factorization of ax <sup>2</sup> +bx+c	
Modeling the Factorization of x <sup>2</sup> +bx+c	
Factoring Special Products	

TOPIC IX	ME NBC LEARN K-12	
VIDEO TITLE		
Scientists Issue Dire Warning About Global Warming		
European Weather Forecasts Superior to U.S. Models		
IMAGE		

TOPIC IX	DISCOVERY EDUCATION CORRELATION			
VIDEO TITLE				
Reviewing Polynomials: Multiplying Negative & Positive Signs				
Illustrating Rules with Example Problems				
Another Method of Multiplying: Lining Up the Expressions				
From Factoring Numbers to Factoring Polynomials				
Applying the Distributive Law to Factoring				

Algebra I		Course Code: 120031001	
TOPIC IX	DISCOVERY EDUCATION CORRELATION		
Factoring with the C	Coefficients of Terms		
Factoring by Inspec	<u>tion</u>		
Introduction: Radica	al Hiking Shortcut		
SKILL BUILDER			
Tile Trials: Modeling	g and Adding Polynomials		
MODEL LESSON			
Powerful Polynomials: Session 2: Polynomial Interpretation			
Powerful Polynomials: Session 3: Functional Factors			
Polynomials Are Everywhere!: Session 2: Quadratic Flight			
MATH OVERVIEW			
Algebra I: Adding ar	nd Subtracting Polynomials		
Algebra I: Modeling	Polynomial Multiplication		

Algebra I	Course Code: 120031001				
Date	Pacing Guide Standards	Data Driven Standard(s)	Activities	Assessment(s)	Strategies
Traditional 21 days Blocks 10 days 01/29/14-02/28/14	MA.912.A.4.1 (EOC) MA.912.A.4.2 (FI, EOC) MA.912.A.4.3 (EOC) MA.912.A.4.4 (EOC)				